Machine Learning for Radiomics

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Outline

- Introduction
- Data Curation
- Training, Validation, and Test datasets
- Linear and Logistic Regression
- Discriminant Analysis
- Penalized Regression (Ridge and Lasso)
- Support Vector Machines
- Decision Trees and Random Forests
- Clustering Methods
- Final Remarks

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What is Machine Learning

- "Machine learning is a field of study that gives computers the ability to learn without being explicitly programmed"
 - Arthur Lee Samuel 1959



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- Develop systems that can automatically adapt and customize themselves to individual users
- Discover new knowledge from large databases (data mining)
- Automate monotonous tasks (which may require some intelligence)
- Develop systems that are too difficult to hard-code because they require specific detailed skills or knowledge relevant to a specific task
 - Knowledge engineering bottleneck

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Why now?

- Large amounts of clinical data
- •Increasing computation power
- Growing progress in available algorithms and theory developed by researchers
- •Increasing support from industries and funding agencies

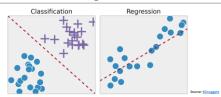
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Supervised vs Unsupervised Learning



Supervised Learning



Goal: to find specific relationships or structure in the input data that allow us to effectively produce correct output data

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Unsupervised Learning



Goal: to learn the inherent structure of our data without using explicitlyprovided labels

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Supervised vs Unsupervised Learning

• Which one should I use??

Supervised Learning

 if you need to train a model to make a prediction--for example, the future value of a continuous variable, such as patient weight or tumor size, or a classification—for example, a segmentation task or HPV status.

Unsupervised learning

• if you need to explore your data and want to train a model to find a good internal representation, such as splitting data up into clusters.

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The two "Trade-offs"

1. Prediction Accuracy vs Model Interpretability

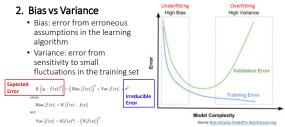
- Global Interpretability
- Local Interpretability
- Feature Selection



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The two "Trade-offs"



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No Free Lunch in ML



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Data Curation

Medical data mining

Linking diseases, drugs, and adverse reactions



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Data Curation



Data Scientist: The Sexiest Job of the 21st Century

Cleaning Big Data: Most Time-Consuming, Least Enjoyable Data Science Task, Survey Says





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Data Curation



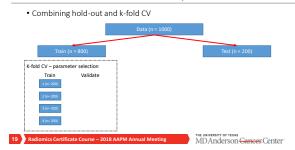
Data Curation Tools

- Information Space: 86 Height Tools for the Data Professional PUS 45 Bonus Tools # Very useful anthology of tools and resources for data professionals, data diabblers, or data scientists from the Syracuse.
- . Digital Curation Resources outside the DCCP Catalog of tools for data creators and digital curators

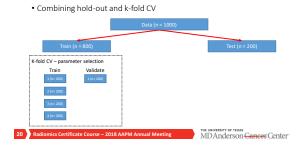
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3.2. Stop training, when a stop-criterion based on E_c^1 is satisfied. 4. For $j = 1, \cdots, m$, evaluate the performance of the final models on T_i : $E_i^1 = error(L_j(T_i))$. **Reformits Certificate Course = 2019 AAPM Annual Meeting** **Distribution Techniques** **MDAnderson Connect Center** **Nore test -> stable estimate of the model error** - Useful when not enough data is available **Algorithm 2 K-fold cross-validation** 1. Input: dataser, T, number of folds k, performance function error, computational models $L_1, \cdots, L_m, m \ge 1$ 2. Divide T into k disjoint substest T_1, \cdots, T_k of the same size. 3. For $i = 1, \cdots, k$: Train model L_i, c, T_i, c, T_i and periodically use T_e to assess the model performance: Train model $L_i, c, T_i, $	 Divide T into three disjoint subsets T_{tr} (training), T_v (validation), and T_t (testing). For j = 1, · · · , m: 3.1. Train model L_j on T_{tr} and periodically use T_v to asses the model performance: 	
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• Useful when not enough data is available Algorithm 2 K-fold cross-validation I. Input: dataset T_i , number of folds k_i performance function $error$, computational models $L_1, \cdots, L_m, m \geq 1$ 2. Divide T into k disjoint subsets T_1, \cdots, T_k of the same size. 3. For $i = 1, \cdots, k$: $T_i \leftarrow T_i T_i \leftarrow \{T \setminus T_i\}$. 3. I. For $j = 1, \cdots, m$: Train model L_j on T_i , and periodically use T_v to asses the model performance: $E_k^{(i)}(i) = error(L_j(T_v))$. Stop training, when a stop-criterion based on $E_k^{(i)}(i)$ is satisfied. 4. For $j = 1, \cdots, m$, evaluate the performance of the models by: $E_v^i = \frac{1}{k} \cdot \sum_{k=1}^k E_v^{(i)}(i)$.	• k-fold cross-validation	
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$E_v^j(i) = error(L_p(T_v)).$ Stop training, when a stop-criterion based on $E_v^j(i)$ is satisfied. 4. For $j = 1, \dots, m$, evaluate the performance of the models by: $E_v^j = \frac{1}{k} \cdot \sum_{i=1}^k E_v^j(i).$ **Recover:		

Cross-validation Techniques



Cross-validation Techniques



Cross-validation Techniques

Combining hold-out and k-fold CV

 Data (n = 1000)

Train (n = 800)

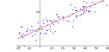
K-fold CV - parameter selection
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Machine Learning Models



Linear Regression

$$Y \approx \beta_0 + \beta_1 X$$



Estimation of Parameters:

Estimation of Parameters: Residuals: $e_l = y_l - \hat{y}_l$ Residual Sum of Squares: $RSS = e_1^2 + e_2^2 + \dots + e_n^2$

Residual sum of squares:
$$ASS = \mathcal{E}_1 + \mathcal{E}_2 + \cdots + \mathcal{E}_n$$
 or $RSS = (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_1)^2 + (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_1)^2 + \cdots + (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_1)^2$ RSS

$$\hat{\beta}_{1} = \frac{\sum_{i=1}^{n} (x_{i} - \bar{x})(y_{i} - \bar{y})}{\sum_{i=1}^{n} (x_{i} - \bar{x})^{2}} \qquad \hat{\beta}_{0} = \hat{y} - \hat{\beta}_{1}\bar{x}$$

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Linear Regression

· Assessing the accuracy of the model

• R-squared or fraction of variance explained

$$R^2 = \frac{\mathrm{TSS} - \mathrm{RSS}}{\mathrm{TSS}} = 1 - \frac{\mathrm{RSS}}{\mathrm{TSS}}$$

$$TSS = \sum_{i=1}^{n} (y_i - \bar{y})^2$$

$$RSS = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$

Residual Sum of Squares

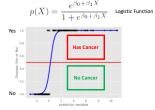
$$\mathrm{RSE} = \sqrt{\frac{1}{n-2}\mathrm{RSS}}$$

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Linear Regression	
* Assumptions * Linear relationship * Residual plots * Multivariate normality (predictors are normally distributed) * Goodness of fit test (Kolmogorov-Smirnov test) * No or little multicollinearity	
Correlation matrix (Pearson's), Tolerance, and variance inflation factor (VIF) No auto-correlation Time-series data Homoscedasticity (residuals are equal across the regression line) Scatter plots	
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La giatia Da guaraja y	
Logistic Regression	
Less assumptions than linear regression Some still apply Observations to be independent of each other Little or no multicollinearity	
 Linearity of independent variables and log odds Larger sample size is useful 	
 The only "real" limitation on logistic regression is that the outcome must be discrete 	
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Logistic Regression	
• Discrete Outcomes (Classification Problem) $p(X)=\frac{e^{\beta_0+\beta_1X}}{1+e^{\beta_0+\beta_1X}} {\rm Logistic Function}$	
Estimation of Parameters:	
Maximum likelihood: $\ell(\beta_0,\beta_1) = \prod_{i:y_i=1} p(x_i) \prod_{i':y_{i'}=0} (1-p(x_{i'}))$ Likelihood Function	
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Logistic Regression

• Discrete Outcomes (Classification Problem)



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Logistic Regression

- Limitations
 - Unstable with well separated classes
 - Unstable with few examples



Discriminant Analysis

Sample average

• Classification algorithm that estimates Bayesian classification

$$\begin{split} \dot{\rho}_k &= \frac{1}{n_k} \sum_{n_k = n_k} x_i & \qquad \delta^x &= \frac{1}{n_k} \sum_{k=1}^K \sum_{n_k < k} (x_i - \hat{\mu}_k)^2 & \qquad \dot{z}_k - n_k / n \\ \\ \textbf{LDA:} & \quad \dot{\hat{\delta}}_k(x) = x \cdot \frac{\hat{\mu}_k}{\hat{\sigma}^2} - \frac{\hat{\mu}_k^2}{2\hat{\sigma}^2} + \log(\hat{\pi}_k) & \quad \text{Discriminant function} \\ \\ \delta_k(x) &= x^T \Sigma^{-1} \mu_k - \frac{1}{2} \mu_k^T \Sigma^{-1} \mu_k + \log \pi_k \end{split}$$

Discriminant Analysis

• Discriminant analysis predicts as follows:

 $\hat{Y}|X=x:=\operatorname{argmax}_k\pi_kp_k(x)=\operatorname{argmax}_k\delta_k(x)$

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Discriminant Analysis

- Key Assumptions
 - Each class density is multivariate Gaussian

$$X|Y_j \sim N(\mu_j, \Sigma_j), \quad j = 0, 1$$

• Equal covariance

$$\Sigma_j = \Sigma, \quad j = 0, 1$$

• No outliers

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Ridge Regression

- \bullet Like least squares linear regression but shrinks the estimated coefficients
- Very useful when multicollinearity (near-linear relationships among the independent variables) occurs
- Given a response vector $y\in\mathbb{R}^n$ and a predictor matrix $X\in\mathbb{R}^{n\times p}$, the ridge regression coefficients are defined as

$$\begin{split} \hat{\beta}^{\text{ridge}} &= \underset{\beta \in \mathbb{R}^p}{\operatorname{argmin}} \sum_{i=1}^n (y_i - x_i^T \beta)^2 + \lambda \sum_{j=1}^p \beta_j^2 \\ &= \underset{\beta \in \mathbb{R}^p}{\operatorname{argmin}} \underbrace{\|y - X \beta\|_2^2}_{\text{Loss}} + \lambda \underbrace{\|\beta\|_2^2}_{\text{Penalty}} \longrightarrow & \mathsf{L_2} \, \mathsf{norm} \end{split}$$

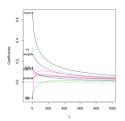
• Where $\lambda \geq 0$ is a tuning parameter that controls the strength of the penalty term

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Ridge Regression
Cannot perform variable
selection

 Coefficients are reduced close to zero, but not zero (unless λ = ∞, where all coefficients are zero)

→ Low interpretability



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Ridge Regression

- •Variable standardization is the first step when using ridge regression!
- Assumptions
 - Linearity
 - •Constant variance (no outliers)
 - Independence

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Lasso

- The Lasso combines some of the shrinking advantages of ridge regression with variable selection
- It is very competitive with the ridge regression in regards to prediction error.
- The only difference between the two is that ridge regression uses ℓ_2 norm penalty where the lasso uses the ℓ_1 norm penalty
- While the ℓ_1 and ℓ_2 norm look very similar, the ridge and lasso solutions behave very differently

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Lasso

• The Lasso (Least Absolute Selection and Shrinkage Operator) is defined

$$\begin{split} \hat{\beta}^{\text{basso}} &= \underset{\beta \in \mathbb{R}^p}{\operatorname{argmin}} \ \|y - X\beta\|_2^2 + \lambda \sum_{j=1}^p |\beta_j| \\ &= \underset{\beta \in \mathbb{R}^p}{\operatorname{argmin}} \ \underbrace{\|y - X\beta\|_2^2 + \lambda}_{\text{Pealty}} + \underbrace{\|\beta\|_1}_{\text{Penalty}} &\longrightarrow \ \mathsf{L}_1 \ \mathsf{norm} \end{split}$$

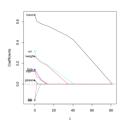
- Again, we have a tuning parameter $\boldsymbol{\lambda}$ that controls the amount of regularization
- As usual, assume $\mathbf{X}^{n \times p}$ is standardize and \mathbf{y} is centered

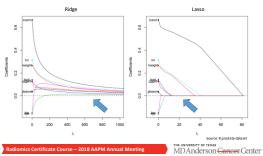
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Lasso

- Often, we believe that many of the β_j 's should be 0
- Therefore, we would like to have a set of **sparse solutions**
- Large enough λ will set some coefficients exactly equal to 0!
 - So the LASSO will perform variable selection for us!

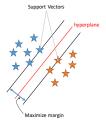




Lasso	
Limitation Cases where p >> n the lasso selects at most n variables before it saturates Convex optimization problem	
Curse of dimensionality Solution	
Elastic Nets (Ridge + Lasso) Zou, Hui; Hastie, Trevor (2005). "Regularization and Variable Selection via the Elastic Net". Journal of the Royal Statistical	
Society. Series B. Wiley. 67 (2): 301–20. JSTOR 3647580	
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Classification w/ Ridge and Lasso	
Add a penalty to the logistic function	
$l_p(\beta_0; \beta; \lambda) = -l(\beta_0; \beta) + \lambda J(\beta)$	-
• Where • $l(\beta_0;\beta)$ denotes the unrestricted log-likelihood function	
• λ is the regularization parameter controlling the amount of shrinkage • $J(\beta)$ is a penalty function on the coefficient parameter β • Either the lasso or ridge penalty functions	
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Support Vector Machines	
Goal: find an optimal hyperplane Support Vectors	
Data points that lie closest to the decision surface (or hyperplane) Most difficult data points to classify They have a direct relationship on the optimal location of the hyperplane	
• In general, there are lots of possible	
solutions • Support Vector Machine (SVM) finds	
an <u>optimal</u> solution	
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Support Vector Machines

- \bullet SVMs $\underline{\text{maximize}}$ the margin around the separating hyperplane
- The decision function is fully specified by a subset of training samples
 - Support Vectors
- Real-world data (non-separable)
 - Soft margin classifier
 - OK to misclassify a few training observations in order to do a better job in classifying the remaining observations



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Support Vector Machines

$$\begin{split} \text{maximize } f(c_1 \dots c_n) &= \sum_{i=1}^n c_i - \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n y_i c_i (\varphi(\vec{x}_i) \cdot \varphi(\vec{x}_j)) y_j c_j \\ &= \sum_{i=1}^n c_i - \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n y_i c_i \underbrace{k(\vec{x}_i, \vec{x}_j)}_{\text{Kernel}} y_j c_j \\ \text{subject to } \sum_{i=1}^n c_i y_i &= 0, \text{ and } 0 \leq c_i \leq \frac{1}{2n\lambda} \text{ for all } i. \end{split}$$

- The Kernel Trick
 - Linear: $k(\overrightarrow{x_i}, \overrightarrow{x_j}) = (\overrightarrow{x_i} \cdot \overrightarrow{x_j})$
 - Polynomial: $k(\overrightarrow{x_i}, \overrightarrow{x_j}) = (\overrightarrow{x_i} \cdot \overrightarrow{x_j})^p$
 - Gaussian radial basis function: $k(\overrightarrow{x_i},\overrightarrow{x_j}) = e^{-\gamma \|\overrightarrow{x_i}-\overrightarrow{x_j}\|^2}$ for $\gamma > 0$
 - Hyperbolic tangent: $k(\overrightarrow{x_i}, \overrightarrow{x_j}) = \tanh(\kappa \overrightarrow{x_i} \cdot \overrightarrow{x_j} + c)$ for some $\kappa > 0$ and c < 0
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Support Vector Machines

- Kernel Trick
 - Useful when the decision function is not linear



Decision Trees	
CART (Classification and Regression Trees, Breiman et al 1984) A decision tree is drawn upside down with its root at the top Node Branches Leaf (decisions) Yes in Radiomics Course? No awake Yes coffee < 2 No awake Wes attention? No	
awake asleep	
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Decision Trees	
How does the algorithm decide which features are more important (top of the tree) and where to create a split?	
Recursive binary splitting All the features are considered and different split points are tried and tested using a cost function	
The split with the lowest cost is selected"Greedy algorithm"	
Cost functions Regression: Mean Square Error	
Classification: Gini, Entropy, etc.	
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Decision Trees	
Improving prediction accuracy • Assigning a maximum depth	
Length of the longest path from the root to leafLeaf size	
 Set a minimum number of training inputs to use on each leaf Pruning 	
 Removal of branches that make use of features having low importance Reduces complexity of the tree → increased predictive power by 	
reducing overfitting • In theory, the depth of the tree is limited by the number of training examples and can be extremely deep	

Decision Trees

- Advantages
 - Simple to understand, interpret, visualize
 - Handles both numerical and categorical data
 - Nonlinear relationships between parameters do not affect tree performance
- Disadvantages
 - Decision tree learners can create over-complex trees → overfitting
 - Decision tree learners create biased trees if some classes dominate Balance the data set prior to training
 - Greedy algorithms cannot guarantee to return the globally optimal decision tree → mitigated by ensemble learning (multiple trees)
 - Adaboost, Bagging, Random Forest, etc.

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Random Forest



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Random Forest

• Adds additional randomness to the model

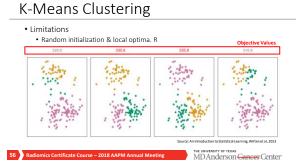


- 1. For each tree: randomly selects a subset of training data (\sim 66%)
- 2. At each node: randomly selects a subset of predictor variables ($\sim \sqrt{p}$)

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Random Forest	
• Out-of-Bag (OOB) Error • Estimates the prediction error of random forests (and other ensemble learners) by using only the trees that did not have a training sample x_i in their bootstrap sample • Feature importance • Very easy to calculate • Can be used to remove low importance features	
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Random Forest	
 Advantages Both regression and classification Easy to use Number of hyperparameters is not too high and they are easy to understand More trees → better predictions (until you reach a plateau) Disadvantages A lot of trees → slow and ineffective for real-time predictions Loss of interpretability 	
Clustering Methods	
 Unsupervised learning technique Helps identify homogenous subgroups or clusters in a data set 	
Two clustering approaches: • K-Means Clustering • Hierarchical Clustering	
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How it works **Appertishin 10.1 is. Moran Chaltering 1. Bendenity worth a transfer, from 1 to 16. To cond of the observations: 2. Beneral until the charter anaginarises due to the victors of the 6. Victors: comparise the charter controls in the 16th charter. (i) Assign each observations in the 16th charter. (ii) Assign each observations in defined village Exclation inflatency. Storace Antibodication Statement Lawreng witness et a. 2013 **Objective Function Objective Function minimizer (\$\frac{1}{\infty} \subseteq \frac{1}{\infty} \subseteq \frac{1



• Creates a dendrogram **Agerithm 10.2 therechold Clustering | Begin with no observations and a measure (sorth as Euclidean distance) of all the (') = n(n-1)/2 poirwise disaminlarities. Treat each observation as its own chatter. 2. For i = n, n-1,..., 2: (a) Examine all pair wise inter-choster dissimilarities among the i chatters and sheriff by the pair of chotters that are least dissimilarity between these two clusters indicates the beight in the dendargement which the fosion double be placed. (b) Compute the new pairwise inter-choster dissimilarities among the i-1 remaining clusters. Source Anistroduction to Statistical Learning, Witten et al., 2013 The advintage of Talas MDA Anderson Center Center' MDA Anderson Center Center'

Clustering Methods	
 Things to remember when using clustering algorithm: 	
 Standardizing variables so that all are on the same scale. It is important when calculating distances 	
 Treat data for outliers before forming clusters as it can influence the distance between the data points. 	
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Honorable Mention List	
 Principal Component Analysis Other Ensemble Methods Bagging and Boosting Nearest Neighbor Naïve-Bayes Classifier 	
Bayesian Networks THE UNIVERSITY OF TEAMS. THE UNIVERSITY OF TEAMS.	
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"Some food for thought"	
• George Box (1919 – 2013)	
"Essentially, all models are wrong, but some are useful"	
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Final Remarks	
Proper splitting of datasets leads to better generalization No peaking at the test set!	
 No one algorithm works best for every problem "No free lunch in Machine Learning" 	
 Think about the inputs in your model Intuition and knowledge about the data can prevent head-aches 	
 Develop a good understanding about mathematical principals behind your algorithm of choice! 	
• Identify the strengths and weaknesses	
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Theodoroul	
Thank you!	
Carlos E. Cardenas, PhD cecardenas@mdanderson.org	
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