#### Model-Based 3D/4D Image Reconstruction: Incorporation of Prior Information

#### Guang-Hong Chen, PhD

Professor of Medical Physics and Radiology



Medical Physics & Radiology UNIVERSITY OF WISCONSIN SCHOOL OF MEDICINE AND PUBLIC HEALTH

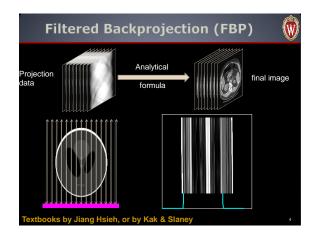
#### Outline

# Ŵ

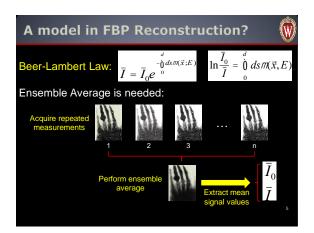
- Model Based Image Reconstruction: Filtered Backprojection (FBP)
- Model based Image Reconstruction: Statistical Model Based Iterative Reconstruction
- Model Based Imaging Reconstruction: Prior Image Constrained Compressed Sensing (PICCS)
- Model Based Image Reconstruction: Beyond the original PICCS
- Discussion and conclusions

# Outline

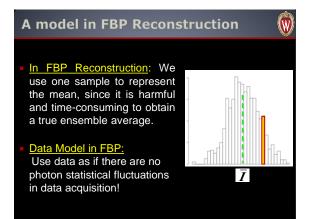
- Model Based Image Reconstruction: Filtered Backprojection (FBP)
- Model based Image Reconstruction: Statistical model based iterative reconstruction (SIR)
- Model Based Imaging Reconstruction: Prior Image Constrained Compressed Sensing (PICCS)
- Model Based Image Reconstruction: Beyond the original PICCS
- Discussion and conclusions

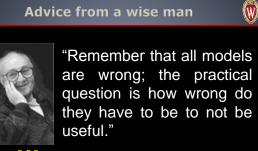






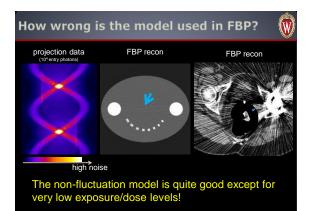






George E. P. Box (1919-2013)

Box, G. E. P., and Draper, N. R., (1987), *Empirical Model Building and Response Surfaces, John Wiley & Sons, New York*, p. 74



#### Outline

# (W)

- Model Based Image Reconstruction: Filtered Backprojection (FBP)
- Model based Image Reconstruction: Statistical Image Reconstruction (SIR)
- Model Based Imaging Reconstruction: Prior Image Constrained Compressed Sensing (PICCS)
- Model Based Image Reconstruction: Beyond the original PICCS
- Discussion and conclusions

#### **Problem statement**

How should we incorporate the actual photon fluctuations into the CT image reconstruction?

W

 For simplicity, let's assume a perfect photon counting detector is used (a model again, sorry!).

# Poisson data model for low exposures 🛛 🕅

We cannot perform repeated measurements to obtain the experimental mean, but what else do we know about the measurement?

#### Probability!



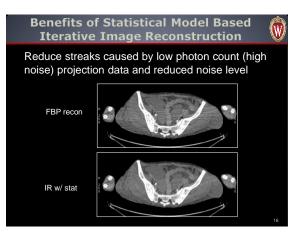
# Inverse problemWhat is the probability to estimate one attenuation<br/>distribution of an image object given that the measured<br/>data set in your hand?Bayesian<br/>rule $P(\{N_i\} \mid m) \vDash P(m \mid \{N_i\}) = \frac{P(\{N_i\} \mid m)P(m)}{P(\{N_i\})}$ Image Reconstruction problem statement:<br/>Seek for an estimation to maximize the probability!

Maximum Likelihood (ML) method 
$$\widehat{W}$$
  
• Maximizing the Log-likelihood function:  
 $\widehat{m} = \arg\max_{m} [\inf_{i=1}^{M} (-\overline{N}_{i} + N_{i} \ln \overline{N}_{i} - \ln N_{i}) + \ln P(m)]$   
• Under the following quadratic approximation:  
 $\widehat{m} := \arg\min_{m} [\frac{1}{2} (\overrightarrow{y} - A\overrightarrow{m})^{T} D(\overrightarrow{y} - A\overrightarrow{m}) + /R(\overrightarrow{m})]$   
 $D = diag\{N_{1}, N_{2}, \dots, N_{M}\}$ 

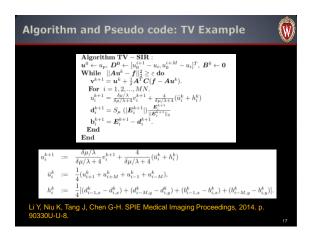
Data model an	d forward projection  🔞
$v_{L} = \ln \frac{I_0}{\pi}$	$ \overset{d}{\underset{0}{\atop0}{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\atop\\{0}{\atop0}{\overset{d}{\underset{0}{\atop\\{0}{\atop0}{\atop\\{0}{\atop0}{\atop\\{0}{\atop1}{\atop\\{0}{\atop1}{\atop1}}}}}}}}}}}}}}}}}} \\{\overset{d}{\underset{0}{\overset{d}{\underset{0}{\atop\\{0}{\atop1}{\atop\\{0}{\atop1}{\atop1}{\atop1}}}}}}}}}}}}\\{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop1}}}}}}}}}\\{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop1}}}}}}}}}}}}\\{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{1}}}}}}}}}}}}}}}}}}\\{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{1}}}}}}}}}}}}}}}\\{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{1}}}}}}}}}}}}}}}}}}}\\\\\overset{d}{\underset{0}{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{1}}}}}}}}}}}}}}}}}\\\\\overset{d}{\underset{0}{\overset{d}{\underset{0}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{1}}}}}}}}}}}}}}}}\\\\\overset{d}{\underset{0}{\atop_{j}}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{j}{\atop_{j}}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{i}{\atop_{j}{\atop_{j}{i}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{i}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{i}{\atop_{j}{\atop_{j}{i}{\atop_{j}{i}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{\atop_{j}{i}{\atop_{j}{i}{\atop_{j}{i}{i}{\atop_{j}{i}{\atop_{j}{i}{\atop_{j}{i}{i}{i}{i}{i}{i}{i}{i}{i}{i}{i}{i}{i}$
represent the me	in FBP: Acquire a single sample to an since it is harmful and time- in the experimental mean.
Iterative Reconstru	el in <u>Statistical Model Based</u> <u>ction:</u> Statistical fluctuations in e considered in data usage!

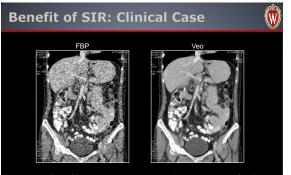
Alternating image update and denoising 
$$\widetilde{m}$$
:=  $\underset{m}{\arg\min} [\frac{1}{2} (\vec{y} - A\vec{m})^T D(\vec{y} - A\vec{m}) + /R(\vec{m})]$   
Data consistency driven image update:  
 $\vec{v}_{k+1} = \vec{m}_k + PA^T D(\vec{y} - A\vec{m}_k)$   
Denoising:  
 $\vec{m}_{k+1} = : \arg\min_{m} \left\{ \frac{1}{2} \parallel \vec{m} - \vec{v}_{k+1} \parallel_{P^{-1}}^2 + /R(\vec{m}) \right\}$   
Combettes and Wijs, Multiscale Model. Simul., Vol. 4: 1168(2005)  
L'Y, Nu K, Tang J, Chen G-H. SPIE Medical Imaging Proceedings, 2014. p.  
90330U-08.

5

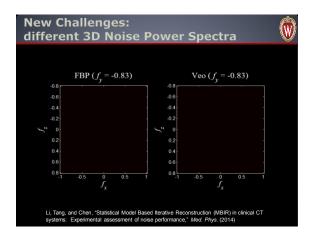




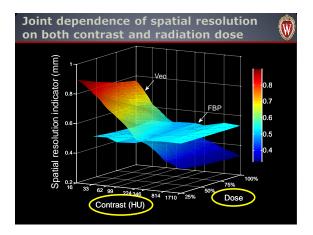




This Abdomen/Pevis CT scan covers ~40 cm in the z direction with a 0.7 mSv effective dose. The BMI of this patient is 19.4.









# Outline

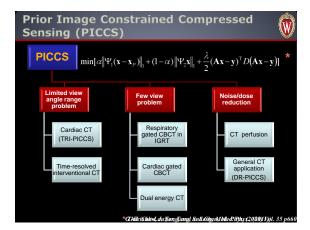
- Model Based Image Reconstruction: Filtered Backprojection (FBP)
- Model based Image Reconstruction: Statistical Image Reconstruction (SIR)
- Model Based Imaging Reconstruction: Prior Image Constrained Compressed Sensing (PICCS)
- Model Based Image Reconstruction: Beyond the original PICCS
- Discussion and conclusions

#### **Problem statement**

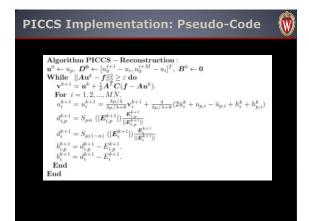
Besides statistics, if we know a portion of image, or a low spatial resolution representation of an image, or low temporal resolution representation of an image, or even an image with lower energy spectral fidelity, can we incorporate this prior images into reconstruction process?

W

We define these low resolution images as our prior image.







#### Computational challenge in IR

- Projection data: M (~10<sup>8</sup>) (1000x1000x64)
- Image data: N (~10<sup>8</sup>) (512x512x400)
- Transform between projection and image domains: M×N
- A full iterative reconstruction method solves a problem of the size of M×N! (Due to sparsity the actual size is ~10<sup>11</sup>)
- Computation time is long without additional innovation/reformulation (Veo takes ~ 1 hour for a typical image volume of 300-400 slices)

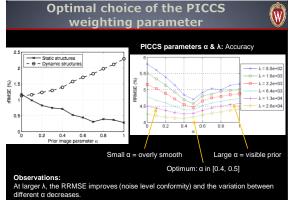
#### Make recon faster: GPU acceleration

- PICCS has special mathematical structures which enable numerical implementations that enjoy both:
- fast convergence speed
- and high parallelizability.
- General purpose graphic cards are used to accelerate the algorithm:
- Clinical CT volumes can be reconstructed within 1~2 minutes



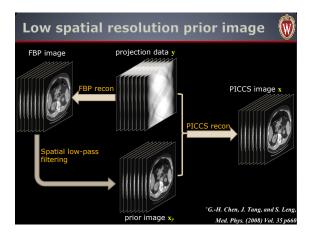
Ŵ

W

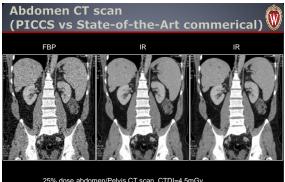


Thèriault-Lauzier, Tang, and Chen, Med. Phys., (2011)

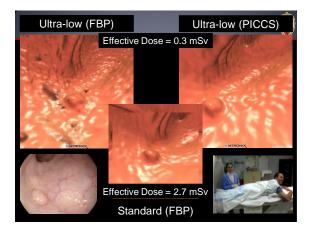




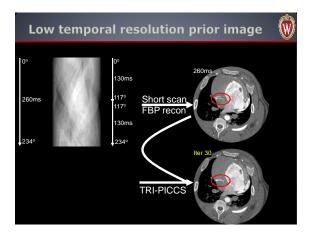




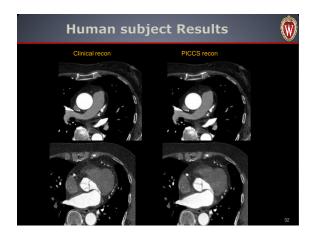
25% dose abdomen/Pelvis CT scan, CTDI=4.5mGy Recon time: 90 minutes for Veo vs 2 minutes for PICCS



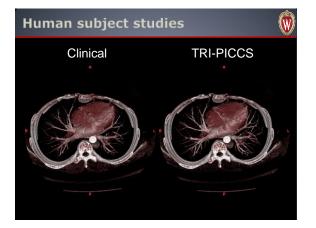




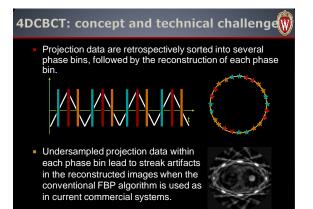


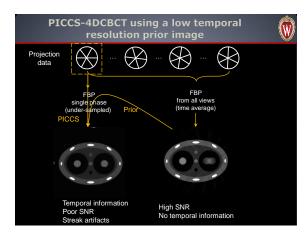




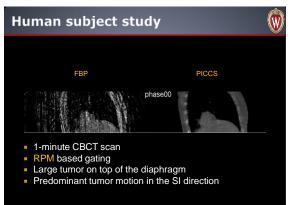


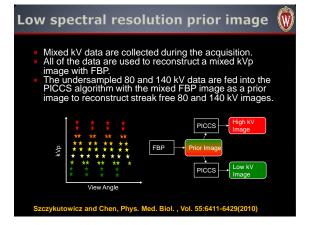


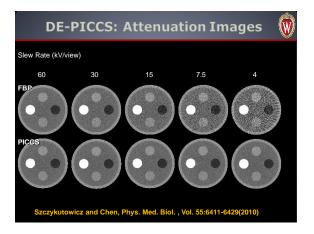


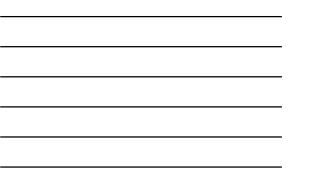








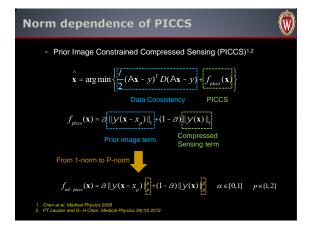




#### Outline

# (W)

- Model Based Image Reconstruction: Filtered Backprojection (FBP)
- Model based Image Reconstruction: Statistical Image Reconstruction (SIR)
- Model Based Imaging Reconstruction: Prior Image Constrained Compressed Sensing (PICCS)
- Model Based Image Reconstruction: Beyond the original PICCS
- Discussion and conclusions





#### Norm dependence in PICCS

- When the selected norm is higher than 1, it has been suggested that a reweighted scheme may be applied to approximate the result achieved with the L1-norm.
- Thus, an iterative reweighted technique is also applied to study the norm dependence of the performance of PICCS.

Gorodnitsky and Rao, IEEE Tran. Signal Processing, Vol.45:600 (1997) Jung, Ye, and Kim, Phys. Med. Biol., Vol. 52:3201(2007) Candes, Wakin, and Boyd, J. Fourier Anal. Applications, Vol.14:877(201

#### **Reweighted p-norm PICCS**

#### W

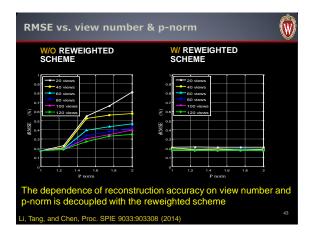
W

Question to be addressed:

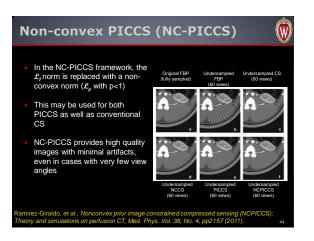
kt

can we replace the 1-norm by a reweighted p-norm in PICCS?

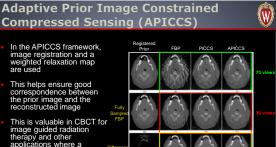
$$\text{iteration:} \quad \overset{\circ}{a}_{i} \frac{f^{p}}{f_{k-1}^{p-1}} \quad \equiv \quad \|f\|$$







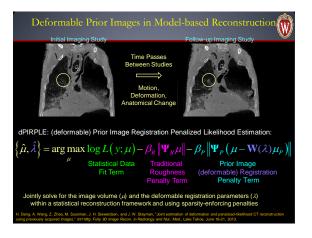




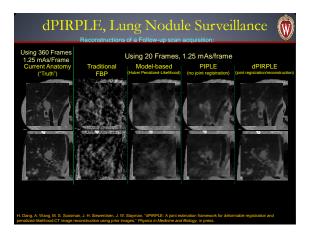
This is valuable in CBCT for image guided radiation therapy and other applications where a perfectly co-registered prior image may not be available

Nett et al, Proc. SPIE 72582: 725803 (2009)

ee, et al. (2012), Improved compressed sensing-based one-beam CT reconstruction using adaptive prior image constraints, Phys. Med. and Biol. Vol. 57, pp2287.









#### **Discussion and conclusions**

- Introduction of statistical model enables improved CT image reconstruction at low photon counts scenarios;
- Introduction of low resolution prior images together with statistical models help further improve CT image reconstruction in a few clinical scenarios;
- Image quality assessment should be performed with care, it is highly recommended to have imaging task in mind for quality assessment.

# Model-Based Image Reconstruction

"Essentially, all models are wrong; but some are useful."

W

Box, G. E. P., and Draper, N. R., (1987), *Empirical Model Building and Response* Surfaces, John Wiley & Sons, New York, p. 424

#### Acknowledgements

Medical Physics: Jie Tang, Shuai Leng, Brian Nett, Zhihua Qi, Pascal Thèriault-Lauzier, Tim Szczykutowicz, Steve Brunner, Ke Li, Kai Niu, Yinsheng Li, John Garrett, Nick Bevins, Joe Zambelli, and Ranjini Tolokanahali.

Radiology Department: Perry Pickhardt, Meg Lubner, David Kim, Chris Francois, Jeff Kanne, Cris Myer, Mark Schiebler, Tom Grist, Howard Rowley, Pat Turski, Charlie Strother, and Bev Kienietz

Human Oncology: Minesh Mehta, George Cannon, Mark Ritter, Lauren Shapiro, Jeni Smilowitz, Bhudatt Pawliwal, and John Bayouth



#### Computational challenge in IR

- Projection data: M (~10<sup>8</sup>) (1000x1000x64)
- Image data: N (~10<sup>8</sup>) (512x512x400)
- Transform between projection and image domains: M×N
- A full iterative reconstruction method solves a problem of the size of M×N! (Due to sparsity the actual size is ~10<sup>11</sup>)
- Computation time is long without additional innovation/reformulation (Veo takes a few hours for a typical image volume of 300-400 slices)

#### Make recon faster: GPU acceleration

- PICCS has special mathematical structures which enable numerical implementations that enjoy both:
- fast convergence speed
- and high parallelizability.
- General purpose graphic cards are used to accelerate the algorithm:
- Clinical CT volumes can be reconstructed within 1~2 minutes



W

W



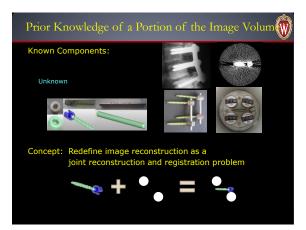
idea. reformulate the constraint into a penality term

$$f_{uc} = \frac{f_{piccs}(\mathbf{x})}{|\psi(\mathbf{x}_{\mathbf{p}})|_{\ell_1}} + \frac{\lambda}{2} \frac{\|\mathbf{A}\mathbf{x} - \mathbf{y}\|^2}{\|\mathbf{A}\mathbf{x}_{\mathbf{p}}\|^2}.$$
  
argmin  $f_{uc}$ .

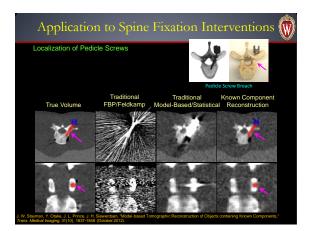
Data consistency term

 $\alpha$ : PICCS parameter a.k.a prior image parameter  $\lambda$ : data consistency parameter

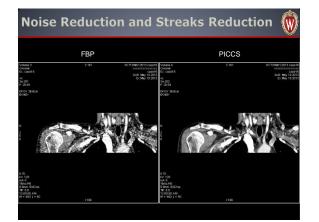
Thèriault-Lauzier, Tang, and Chen, Med. Phys., (2011)



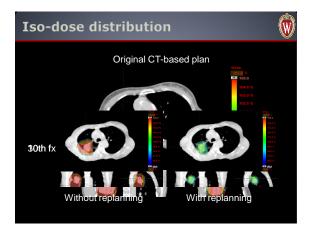


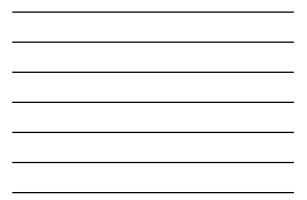


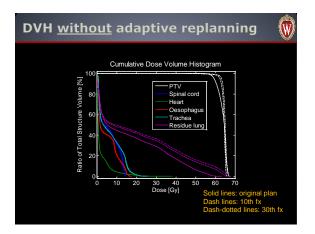




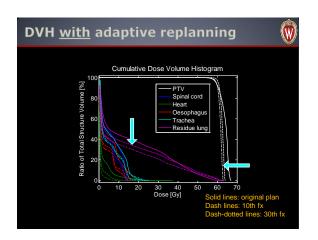




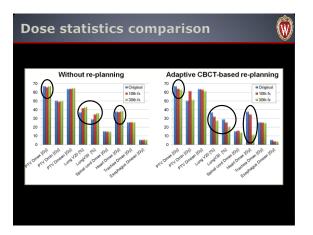




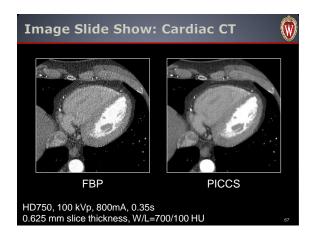


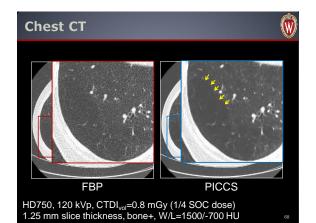


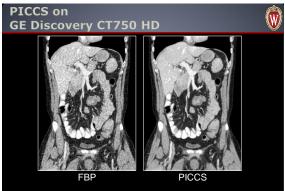




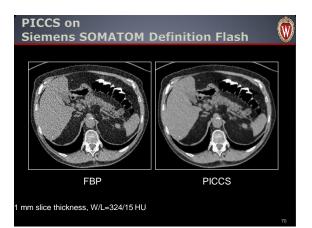


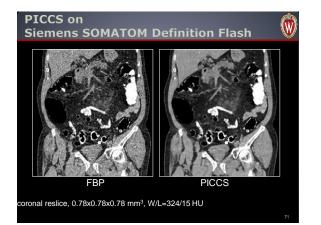


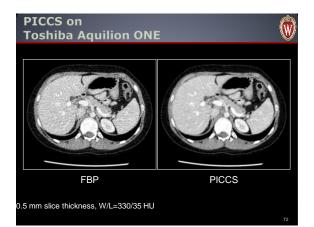




120 kVp, CTDI<sub>vol</sub> 5 mGy. coronal reslice, 0.66x0.66x0.66 mm³, W/L=324/15 HU





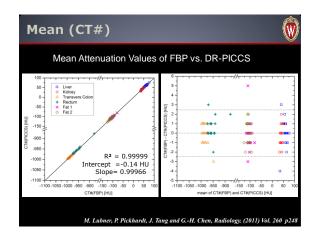




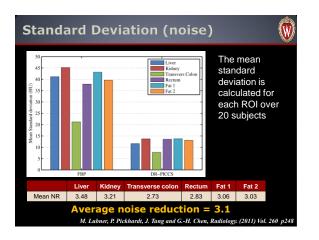
# Retrospective study design

- 20 human subjects CT colonoscopy cases
- Six 100 mm<sup>2</sup> ROIs were measured for each case
- 2 from air (inside colon)
- 2 from fat
- 1 from kidney
- 1 from liver
- Images have been read by radiologists who confirmed there were no small structure losses \*

M. Lubner, P. Pickhardt, J. Tang and G.-H. Chen, Radiology. (2011) Vol. 260 p248









# Outline

- Iterative reconstruction (IR) methods
- PICCS, a UW-brand IR method, for low dose CT
- Prospective low dose: clinical evaluation
- Challenges and perspectives

#### Prospective low dose study

Common limitations in most current low dose results:

W

W

W

- Lack of solid diagnostic value evaluation
- Retrospective study with low dose methods applied on normal dose scans
- Lack of truth in low dose scans
- Very limited number of low dose scans
- A prospective low dose clinical trial with normal dose scan as reference and sufficient number of subjects is needed to validate how low dose techniques should be utilized to benefit clinical diagnosis.

#### Study design – scan and recon

- A low-dose CT series was acquired immediately following the routine standard-dose CT series (HIPAA-compliant, IRB approved protocol)
- Targeted dose reduction 70%-90%
- Ultimate goal 500 subjects Initial results included 45 subjects
- Low-dose scans were reconstructed using FBP, ASiR(40%), Veo, PICCS – for evaluation
- Standard-dose scans were reconstructed using FBP – as reference

P. Pickhardt, M. Lubner, D. Kim, J. Tang, R. Julie, A. Munoz del Rio and G. Chen., AJR. (2012) Vol. 199

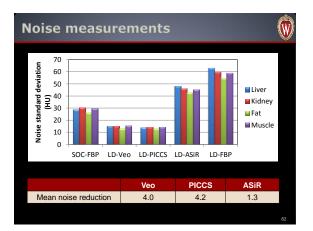
#### Study design – results analysis

#### Image reformat

- Reconstructed images were reformatted into 2.5 mm thickness axial and coronal series for review
- Quantitative measurements (four 250 mm<sup>2</sup> ROIs)
   liver, kidney, muscle, and fat
- Clinical evaluation
  - All images were de-identified and randomized with respect to patients and reconstruction methods.
  - Two expert radiologists reviewed all low-dose series first, then reviewed standard-dose series to serve as clinical reference standard.
  - The results were pooled together from both readers.

Mean	(CT#):	Bland-Al	tma	n plots	Ŵ		
Bland-A	Bland-Altman analysis on low-dose scans						
	Bias (HU)	Limits (HU)		24 • • • • • • • • • • • • • • • • • • •	· · · ·		
ASiR	0	0.8		20- 19- 18-	-		
PICCS	0	2.6		17- 16- 15-			
Veo	4.3	8.5					
ACR	ACR QC: CT#(water) = 0±7 HU Uniformity within ±5 HU						
CT4(FB)-CT1A(SIR) [Hu]							
ASIR PICCS				Veo	81		

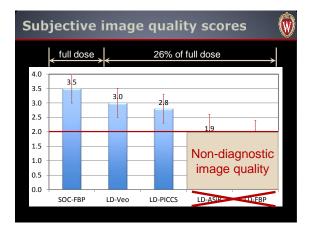






# Qualitative image quality score criteria: 5-point scale

- 0: non-diagnostic
- 1: severe artifact with low confidence
- 2: moderate artifact or moderate diagnostic confidence
- 3: mild artifact or high confidence
- 4: well depicted without artifacts



#### Lesion detection tasks:

- Low contrast lesion detection:
  - Soft-tissue window: W/L=400/50 HU
  - Non-calcific detectable organ-based foci >3 mm

- High contrast stone detection:
  - Bone window: W/L=1200/350 HU
  - Stones >2 mm

