

# Modeling of MR-guided HIFU for Breast and Brain Therapy

Douglas Christensen

*Department of Bioengineering  
Department of Electrical & Computer Engineering*

*University of Utah  
Salt Lake City, UT 84112*

Utah Center for Advanced Imaging Research



UNIVERSITY OF UTAH  
SCHOOL OF MEDICINE

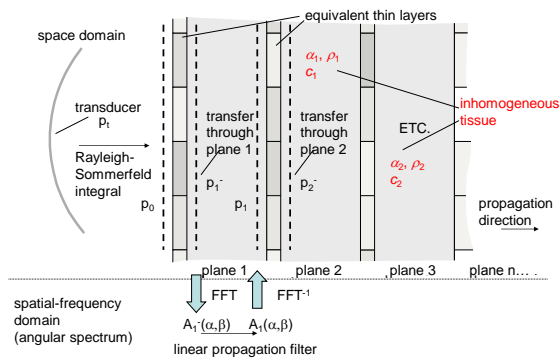
## Outline of Talk

- Overview of Hybrid Angular Spectrum (HAS) method
- Three examples of use:
  1. Modeling of acoustic radiation force imaging (ARFI)
  2. Determining extent of phase aberration in breast treatments
  3. Predicting heating efficiency in transcranial treatments (on-going)

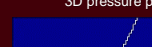
## Concept of Hybrid Angular Spectrum Method\*

- Extends traditional angular spectrum method (in spatial-frequency domain) to include inhomogeneous media
- Leapfrogs between the space and spatial-frequency domains (next slide)
- Employs FFT commands, so very rapid
- Assumptions: steady state conditions, linearity and compressional waves only

\*U. Vyas and D. A. Christensen, "Ultrasound beam simulations in inhomogeneous tissue geometries using the hybrid angular spectrum method," *IEEE Trans UFFC* 59 (6), 1093-1100, June 2012.



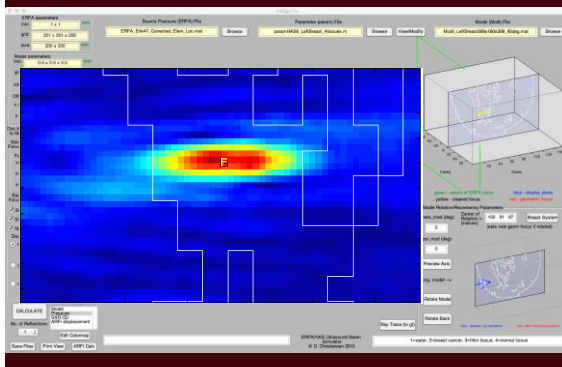
## HAS Method Overview

- Comparable to FDTD results within 2.8% (3D breast model)\*
  - Two orders of magnitude faster\*:  
FDTD – 67 min      HAS – 9.6 s
  - Example simulation:  
3.5 MHz      beam →  
3D model 141 x 141 x 161
- 

\*U. Vyas and D. A. Christensen, *IEEE Trans UFFC* 59 (6), 1093-1100, June 2012.



HAS gui Screen Shot with Typical Pressure Pattern



## Example 1 – ARFI Modeling

Study by Allison Payne with Josh de Bever et al.\*

Uses –

- Finding location of beam focus in any tissue (e.g., replaces thermal test shot in fatty tissue)
- Determining mechanical properties of tissue (e.g., for treatment assessment)

\*A. Payne, J. de Bever, A. Farrer, B. Coats, D. Parker and D. Christensen, "A simulation technique for 3D MR-guided acoustic radiation force imaging," *Med. Phys.* 21(2), Feb 2015.

---

---

---

---

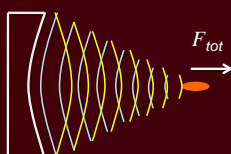
---

---

---

---

## Origin of Radiation Force



$$\bar{F}_{abs} = \frac{2\alpha I}{c} \quad \frac{\text{N}}{\text{m}^2}$$

$$\bar{F}_{ref} = \frac{2IR^2}{c} \quad \frac{\text{N}}{\text{m}^2}$$

$I$  = intensity from HAS calculation  
 $\alpha$  = tissue absorption coefficient  
 $R$  = interface reflection coefficient  
 $c$  = speed of sound

$$F_{tot} = \int \int \int \bar{F}_{abs} + \int \int \bar{F}_{ref} \quad [\text{N}]$$

---

---

---

---

---

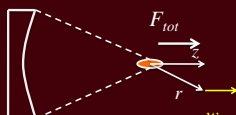
---

---

---

## Generation of Displacement $w$ due to Distributed Force

Simplifications: Elastic medium, so  $\lambda \gg \mu$



$$w = \frac{1}{8\pi\mu} \left[ \frac{z^2}{r^3} + \frac{1}{r} \right] \otimes F_{tot}$$

$\lambda$  = first Lamé coefficient  
 $\mu$  = Lamé shear coefficient

$g(r)$  (green arrow) and  $\otimes F_{tot}$  (yellow circle) are labeled as **distributed force field**.

- 3D green's function  $g(r)$  is convolved with distributed force field (computed using the HAS technique)
- Carried out in frequency domain

---

---

---

---

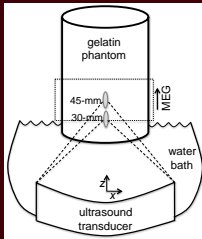
---

---

---

---

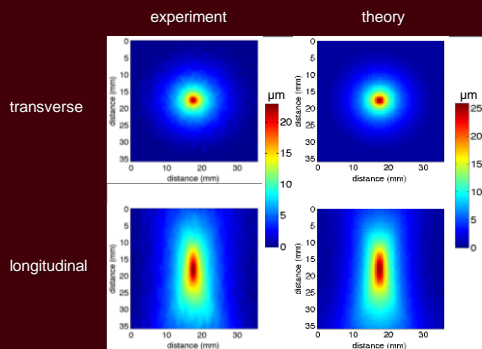
## Experimental Validation with MRI



- Three different values of gelatin stiffness (Young's modulus) used: 125, 175 and 250 bloom
- Young's modulus, speed of sound and attenuation independently measured (similar to soft tissue values)
- Displacement in 3D volume determined by MR phase measurements\*
- Ultrasound on for 10 ms at 66 W.

\* J. de Bever, N. Todd, M. Diakite, D. Parker, Proceedings of the ISMRM 21st Scientific Meeting, Salt Lake City, USA, 20-26 Apr., 2013.

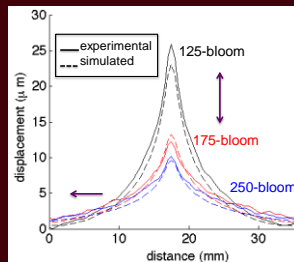
## Results – Displacement for 125 bloom



## Results – All three bloom values

Notes:

- Peak displacement inversely related to Young's modulus (bloom value)
- Displacement shape broadens for faster shear wave speed (higher Lamé coefficient)



transverse slice, 30-mm focus depth

## Example 2 – Determining Extent of Phase Aberration in Breast Treatments

Study by Allison Payne with Alexis Farrer and Chris Dillon et al.\*

### Motivation –

- Phase aberration is a known issue in HIFU with large-aperture transducers (e.g., transcranial)
- Extent of phase aberration is unknown for smaller aperture transducers (e.g., Utah breast system)

\*A. Farrer, S. Almquist, C. Dillon, D. Parker, D. Christensen and A. Payne, "Phase aberration simulation study of MRgFUS breast treatments," 15th International Symposium on Therapeutic Ultrasound, Utrecht, Apr. 15-18, 2015

---

---

---

---

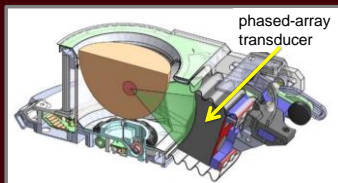
---

---

---

---

## Utah MRgFUS Breast System



---

---

---

---

---

---

---

---

## Goals of Breast Study

- Determine if phase aberrations will be present for our smaller aperture transducer through HAS-simulated treatments
- Investigate how the treatment will benefit from phase aberration correction in the presence of various degrees of breast heterogeneity

---

---

---

---

---

---

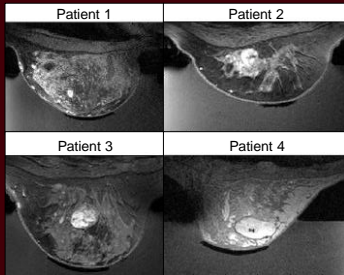
---

---

## MRI Patient Data

4 female volunteers with fibroadenoma(s)

- 18 to 45 years old
- 1 to 8 fibroadenomas per patient
- 3-point Dixon acquisition
- Contrast-enhanced T1-weighted images




---

---

---

---

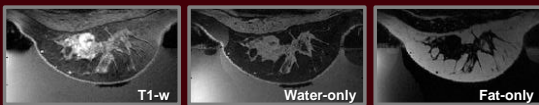
---

---

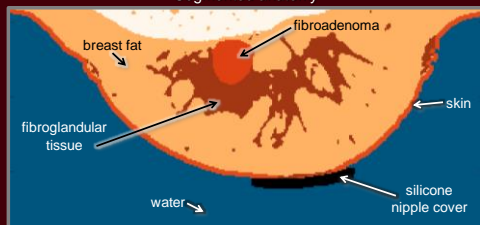
---

---

## Segmentation



Segmented anatomy




---

---

---

---

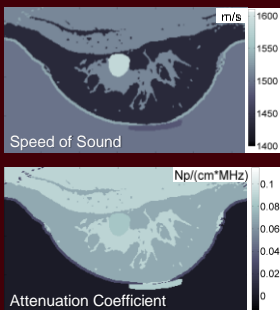
---

---

---

---

## Acoustic Simulations



- Acoustic properties determined from Duck et al. 1990\*
- 0.5-mm isotropic resolution
- Hybrid Angular Spectrum (HAS) method employed to give SAR pattern

\* FA Duck, *Physical Properties of Tissues*, Academic Press: Harcourt Brace Jovanovich, 1990.

---

---

---

---

---

---

---

---

## Treatment Simulation Set-Up

Superior Approach



---

---

---

---

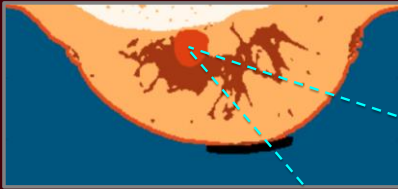
---

---

---

## Treatment Simulation Set-Up

Inferior Approach



---

---

---

---

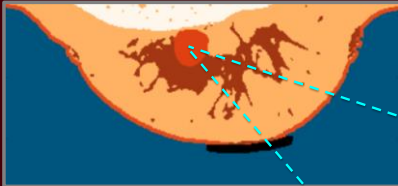
---

---

---

## Treatment Simulation Set-Up

Inferior Approach



---

---

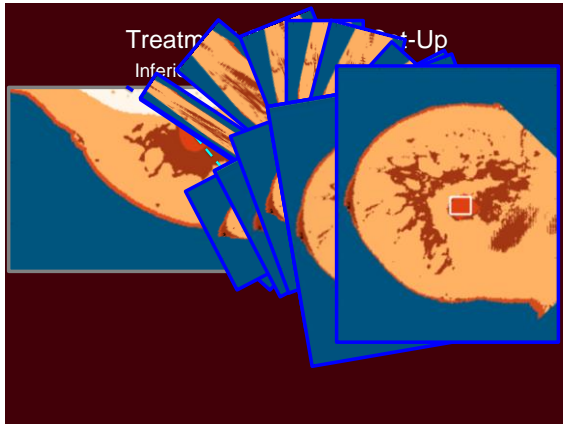
---

---

---

---

---




---

---

---

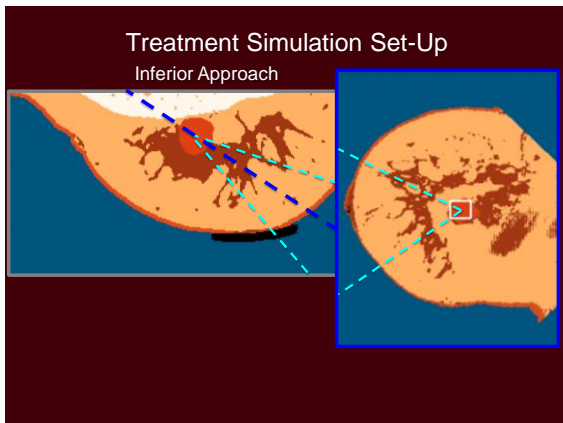
---

---

---

---

---




---

---

---

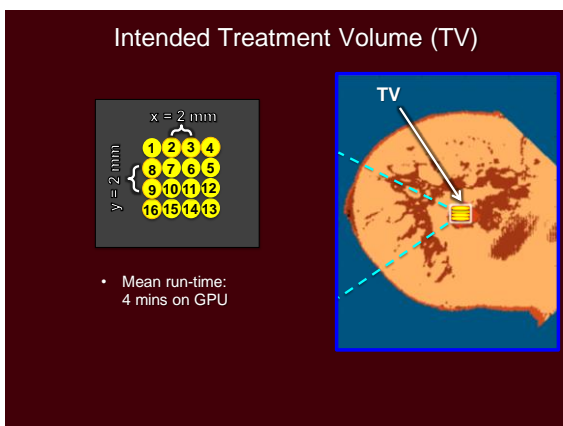
---

---

---

---

---




---

---

---

---

---

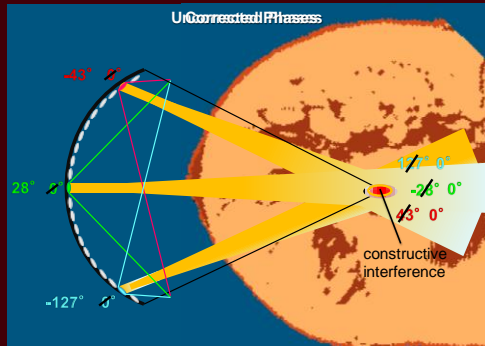
---

---

---



### Phase Correction Approach




---

---

---

---

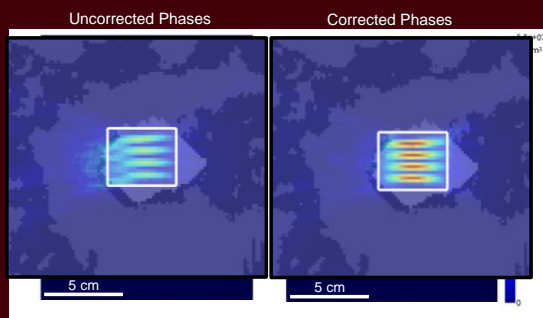
---

---

---

---

### Results: Power Deposition




---

---

---

---

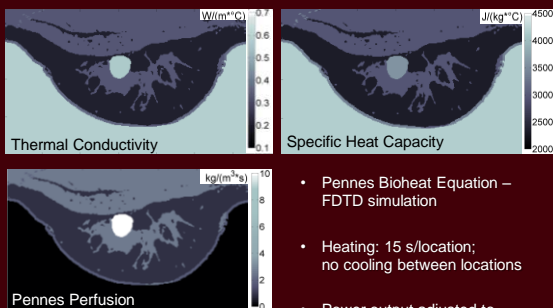
---

---

---

---

### Thermal Simulations



- Pennes Bioheat Equation – FDTD simulation
- Heating: 15 s/location; no cooling between locations
- Power output adjusted to achieve a 20 °C rise at first treatment location

---

---

---

---

---

---

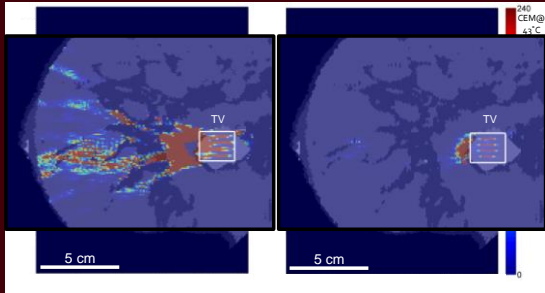
---

---

### Results: Thermal Dose\*

Uncorrected Phases

Corrected Phases



\*S. A. Sapareto and W. C. Dewey, "Thermal dose determination in cancer therapy," Int. J. Radiat. Oncol., Biol., Phys. 10(6), 787-800 (1984).

---

---

---

---

---

---

---

---

---

---

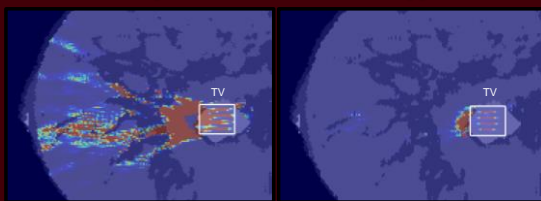
### Dose Volume Ratio Metric

Uncorrected Phases

Corrected Phases

DVR = 9.1

DVR = 3.9



Dose Volume Ratio (DVR):

$$DVR = \text{Volume Outside TV} \geq 240_{CEM} / \text{Volume Inside TV} \geq 240_{CEM}$$

(smaller is better)

---

---

---

---

---

---

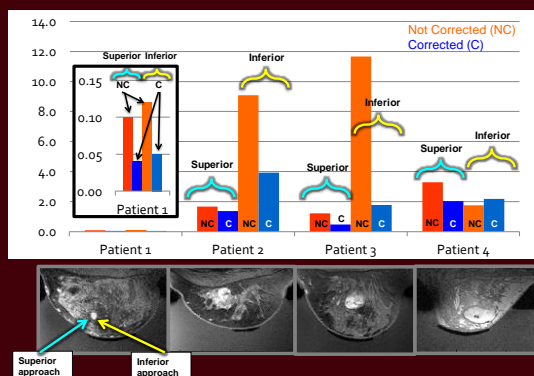
---

---

---

---

### Results: DVR (Dose Volume Ratio)




---

---

---

---

---

---

---

---

---

---

### Example 3 – Predicting Heating Efficiency in Transcranial Treatments

Study by Dennis Parker with Scott Almquist and Henrik Odeen et al.\* (on-going)

#### Background –

- Temperature profiles (space and time) available for 14 patients undergoing transcranial essential tremor treatments
- Perform retrospective analysis of temperature as a function of applied acoustic energy to determine efficiency of heating

\*S. Almquist, N. Todd, J. de Bever, D. Parker and D. Christensen, "Correcting Phase Aberrations in Transcranial High Intensity Focused Ultrasound," International Society for Therapeutic Ultrasound Symposium, Heidelberg, Germany, June 11-13, 2012.

---

---

---

---

---

---

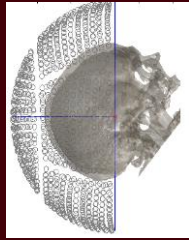
---

---

### Modeling of Transcranial Treatments



InSightec 650-kHz ExAblateNeuro



1024-element applicator in place

---

---

---

---

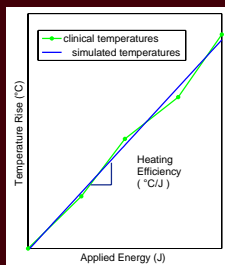
---

---

---

---

### Modeling of Transcranial Treatments



#### Modeling Steps:

- Model skull from CT scan with acoustic values based on Hounsfield Units\*
- Propagate beam into brain with HAS using clinically found element amplitudes and phases
- From HAS SAR pattern, find peak temperature with bioheat equation (FDTD)
- Plot peak temperature as a function of exposure energy: slope = Heating Efficiency ( $^{\circ}\text{C}/\text{J}$ )

\* S. Pichardo, V. W. Sin, and K. Hynnen, *Phys. Med. Biol.*, 56 (1) 219, Jan 2011

---

---

---

---

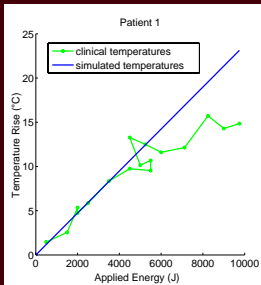
---

---

---

---

Patient 1



Notes:

- Some clinical searching for optimum temperature imaging plane
- Bending over of clinical plot at higher temperatures
- Reasonable simulation match at lower energy levels

---

---

---

---

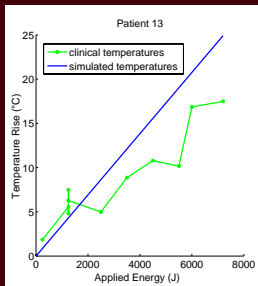
---

---

---

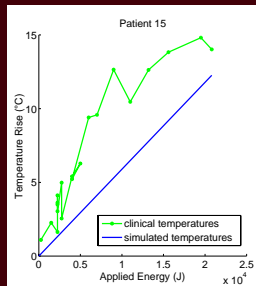
---

Patient 13



Overpredicted

Patient 15



Underpredicted

---

---

---

---

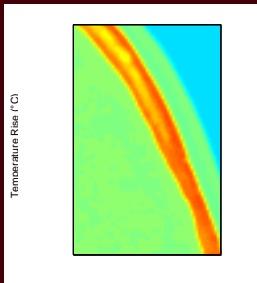
---

---

---

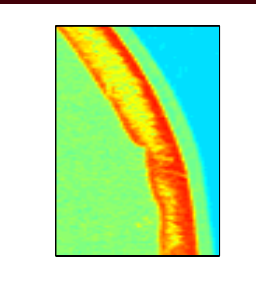
---

Patient 13



Overpredicted

Patient 15



Underpredicted

---

---

---

---

---

---

---

---

## Acknowledgements



Allison Payne, PhD  
 Doug Christensen, PhD  
 Dennis Parker, PhD  
 Bob Roemer, PhD  
 Rock Hadley, PhD  
 Josh de Bever, PhD  
 Henrik Odéen, PhD  
 Chris Dillon, PhD  
 Alexis Farrer, MS  
 Emilee Minalga, MS  
 Scott Almquist, BS  
 Sara Johnson, BS  
 Bryan Smith, BS  
 Matt Holbrook, BS  
 Siemens Healthcare AG  
 NIH grants:  
 R01 CA172787  
 R01 EB013433  
 Image Guided Therapy  
 FUS Foundation

Thank You  
 Any Questions?

Utah Center for Advanced Imaging Research



UNIVERSITY OF UTAH  
SCHOOL OF MEDICINE

Thank You

Any Questions?

Utah Center for Advanced Imaging Research



UNIVERSITY OF UTAH  
SCHOOL OF MEDICINE

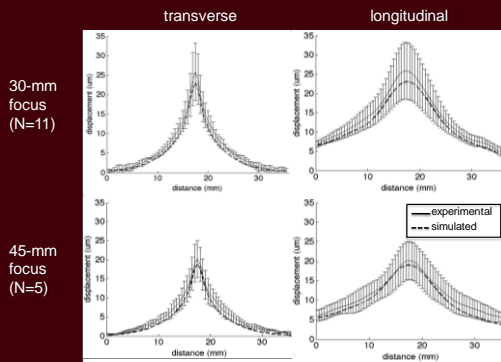
## Numerical Modeling of Focused Ultrasound

### Uses -

- Predicting beam and heating patterns
- Determining phases for aberration correction
- Retrospective analysis of treatments
- Designing custom applicators
- Potential for patient treatment planning

### Limitations -

- Only as valid as model parameters
- Simplifications reduce accuracy
- Need experimental validation

Results – Displacement ( $\mu\text{m}$ ) for 125 bloom


---

---

---

---

---

---

---

---

## Summary – HAS Technique

- HAS method allows rapid beam calculations of pressure, intensity and SAR patterns.
- Includes refraction, attenuation and reflection effects.
- MATLAB gui provides convenient user interface.

## Future work:

- Including shear waves and multiple reflections.
- Adding scattering component to attenuation.

---

---

---

---

---

---

---

---

## Summary – ARFI Modeling (Example 1)

- Developed a numerical model for ARFI displacements
- Force field calculated by the HAS technique
- Validated with 3D MRI displacement measurements
- Model estimates displacements to within 2.8-12 % accuracy

---

---

---

---

---

---

---

---

### Summary – Breast System (Example 2)

- Phase aberration correction improved most treatments for our smaller aperture breast specific system.
- The degree of improvement depends on the amount of tissue heterogeneity in the beam path.

#### Future Work:

- Determine a figure of merit for clinicians that indicates how beneficial patient-specific phase correction will be.

---

---

---

---

---

---

---

### Summary – Transcranial (Example 3)

- aaa
- Bbb

#### Future Work:

- ccc

---

---

---

---

---

---

---